

Phil 225 Spring 2012  
HW 2, Due 2/10/12

- 1) For each of the sentences given and the interpretation following, say whether the sentence is true where  $D = \aleph$  (the natural numbers). Then do the same where  $D = \Re$  (the real numbers). Remember that  $\aleph$  includes 0. You may want to make a table for your answers.

$$L^2: \{ \langle x, y \rangle \mid x < y \}$$

$$I^2: \{ \langle x, y \rangle \mid x = y \}$$

$$S^3: \{ \langle x, y, z \rangle \mid x + y = z \}$$

$$P^3: \{ \langle x, y, z \rangle \mid x \cdot y = z \}$$

$$a_4:4 \quad a_{10}:10$$

- a)  $(\forall x)(\exists y)Lxy$
  - b)  $(\forall x)(\exists y)Lyx$
  - c)  $(\forall x)(\forall y)[Lxy \rightarrow (\exists z)(Lxz \wedge Lzy)]$
  - d)  $(\forall x)(\exists y)Ixy$
  - e)  $(\forall x)(\forall y)(\exists z)Sxyz$
  - f)  $(\forall x)(\forall y)(\exists z)Sxzy$
  - g)  $(\forall x)(\forall y)(\exists z)Pxzy$
  - h)  $(\exists x)(Lxa_4 \rightarrow Sxxa_{10})$
- 2) Chapter 4, ex. 10, a-d.
- 3) For each of the following sets of sentences, show that it is consistent by giving an interpretation in which all of its members are true.

a)  $(\forall x)(\exists y)Fxy$

$$(\forall x)(\exists y)\neg Fxy$$

$$(\forall x)(\forall y)(Fxy \rightarrow \neg Fyx)$$

b)  $(\exists x)(\exists y)(Fxy \wedge Fyx)$

$$(\forall x)(\forall y)(Fxy \rightarrow Fyc)$$

$$(\forall x)(\forall y)(Fxy \rightarrow (Gy \rightarrow (\exists z)Fyz))$$

$$(\forall x)(\exists y)\neg Fxy$$